

maTema t i ka

bi znes is aTvis

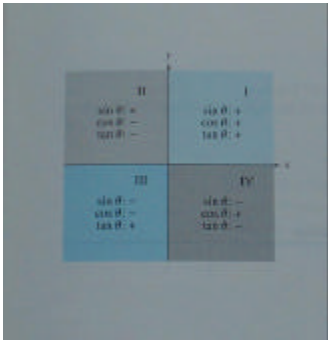


Tbi l i si
2007

a l g e b r a

Semoklebuli gamravlebis formulebi	proporciebi
$a^2 - b^2 = (a - b)(a + b)$ $a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)$ $(a \pm b)^2 = a^2 \pm 2ab + b^2$ $(a \pm b)^3 = a^3 \pm 3a^2b + 3ab^2 \pm b^3$ $(a + b + c)^2 = a^2 + b^2 + c^2 + 2ab + 2ac + 2bc$	Tu $\frac{a}{b} = \frac{c}{d}$, მაშინ $ad = bc$ $\frac{d}{b} = \frac{c}{a} \quad \frac{a}{c} = \frac{b}{d} \quad \frac{d}{c} = \frac{b}{a}$ $\frac{a \pm b}{b} = \frac{c \pm d}{d} \quad \frac{a \pm b}{a} = \frac{c \pm d}{c}$ $\frac{a+b}{a-b} = \frac{c+d}{c-d}$
xarixi	moqmedebebi xarisxebze
$a^n = \overbrace{a \cdot a \cdots a}^{n-jer}, n \in N$ $a^0 = 1, a \neq 0$ $a^{-n} = \frac{1}{a^n}, a \neq 0, n \in N$ $a^{m/n} = \sqrt[n]{a^m}, m \in Z, n \in N, a > 0$	$(ab)^n = a^n b^n$ $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}, b \neq 0$ $a^m \cdot a^n = a^{m+n}$ $\frac{a^m}{a^n} = a^{m-n}$ $(a^m)^n = a^{mn}$
kvadratu li gantolebis amonaxsna formula	vietas Teorema
$ax^2 + bx + c = 0, a \neq 0, D = b^2 - 4ac$ $D \geq 0$ $x_{1,2} = \frac{-b \pm \sqrt{D}}{2a}$ $x_{1,2} = \frac{-k \pm \sqrt{k^2 - ac}}{a}, b = 2k$ $D < 0$ kvadratu li gantolebas namdvi l ricxvTa simravleSi amonaxsni ar gaacnia	Tu x_1 da x_2 aris $ax^2 + bx + c = 0$ gantolebis amonaxsni, მაშინ $x_1 + x_2 = -\frac{b}{a}, \quad x_1 \cdot x_2 = \frac{c}{a}$ kvadratu li samwevris daSla maravlebad $ax^2 + bx + c = a(x - x_1)(x - x_2)$
arimetiku li progresia	geometriu li progresia
$a_n = a_1 + (n-1)d; S_n = \frac{2a_1 + (n-1)d}{2} n$ $S_n = \frac{2a_n - (n-1)d}{2} n \quad a_n = \frac{a_{n-1} + a_{n+1}}{2}$	$b_n = b_1 q^{n-1}; S_n = \frac{b_1(q^n - 1)}{q - 1}$ $S_n = \frac{b_n q - b_1}{q - 1} (q \neq 1) \quad b_n^2 = b_{n-1} \cdot b_{n+1}$

t r i g o n o m e t r i a

trigonometriul funciaTa niSnebi	damokidebuleba erTi da igive argumentis trigonometriul funciebs Soris
	$\sin^2 a + \cos^2 a = 1$ $\operatorname{tga} = \frac{\sin a}{\cos a}$ $\operatorname{ctga} = \frac{\cos a}{\sin a}$ $\operatorname{tga} \cdot \operatorname{ctga} = 1$ $1 + \operatorname{tg}^2 a = \frac{1}{\cos^2 a}$ $1 + \operatorname{ctg}^2 a = \frac{1}{\sin^2 a}$
ori argumentis jamisa da sxvaobis trigonometriuli funciebi	naxevari argumentis trigonometriuli funciebi
$\sin(a \pm b) = \sin a \cos b \pm \cos a \sin b$ $\cos(a \pm b) = \cos a \cos b \mp \sin a \sin b$ $\operatorname{tg}(a \pm b) = \frac{\operatorname{tga} \pm \operatorname{tgb}}{1 \mp \operatorname{tga} \operatorname{tgb}}$	$\sin^2 \frac{a}{2} = \frac{1 - \cos a}{2}$ $\cos^2 \frac{a}{2} = \frac{1 + \cos a}{2}$ $\operatorname{tg}^2 \frac{a}{2} = \frac{1 - \cos a}{1 + \cos a}$
ormagi argumentis trigonometriuli funciebi	trigonometriul funciaTa gamosaxva naxevari argumentis tangensi T
$\sin 2a = 2 \sin a \cos a$ $\cos 2a = \cos^2 a - \sin^2 a$ $\operatorname{tg} 2a = \frac{2 \operatorname{tga}}{1 - \operatorname{tg}^2 a}$	$\sin a = \frac{2 \operatorname{tg} \frac{a}{2}}{1 + \operatorname{tg}^2 \frac{a}{2}}$ $\cos a = \frac{1 - \operatorname{tg}^2 \frac{a}{2}}{1 + \operatorname{tg}^2 \frac{a}{2}}$ $\operatorname{tga} = \frac{2 \operatorname{tg} \frac{a}{2}}{1 - \operatorname{tg}^2 \frac{a}{2}}$