



**Flow Measurement Uncertainty:
Standard Deviation and Standard Error of the Mean**

Flow Measurement Uncertainty: Standard Deviation and Standard Error of the Mean



Bassam Al-Otaibi

Kuwait Oil Company

الرعاي الرسمي
OFFICIAL SPONSOR



إمسيو البترول الكويتية مؤسسة البترول الكويتية
Kuwait Petroleum Corporation



MEASUREMENT UNCERTAINTY

M i s c o n c e p t i o n :

- Measurement is an **exact** science.

F a c t s :

- All measurements are merely **Estimates** of the **True** value being measured and yet the true value can never be known.
- The Repeated Measurement of a fixed quantity will **NEVER** yield the same result every time.

MEASUREMENT UNCERTAINTY

Definition:

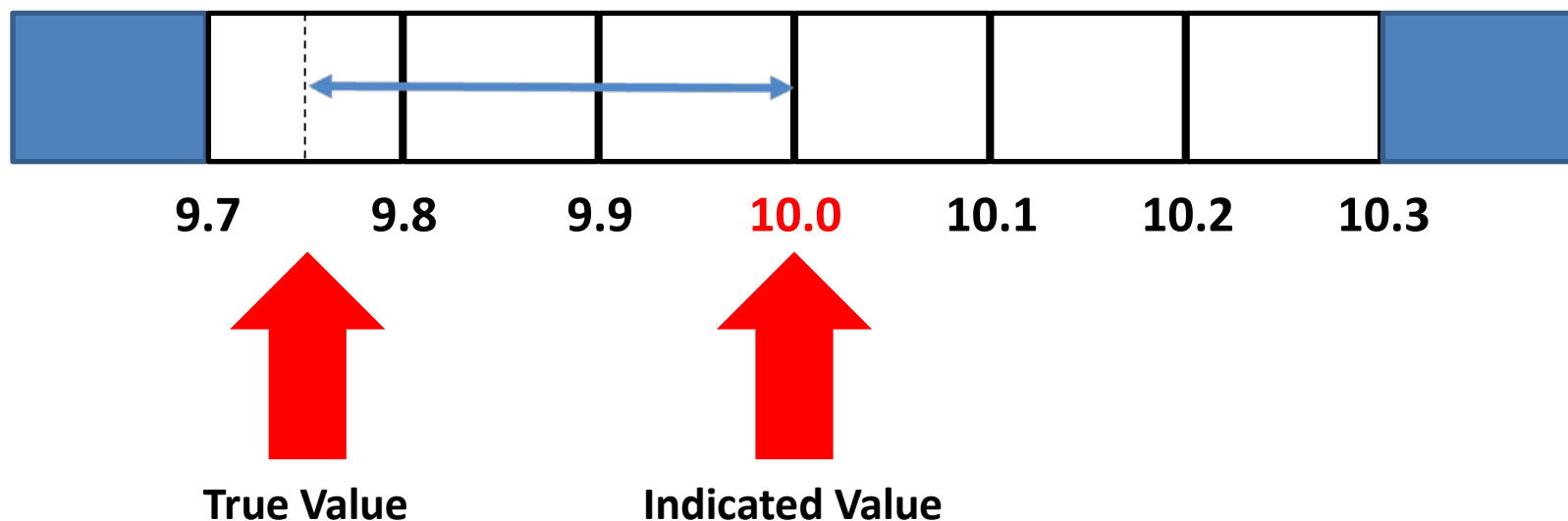
Uncertainty of measurement gives an indication of the **Quality** or **Reliability** of a measurement result.

Hence, Uncertainty is the **margin of doubt** associated with a measurement.

DON'T CONFUSE ERROR WITH UNCERTAINTY!

Error is the **difference** between the measured **value** and the **true** value.

An illustration of measurement error:



Uncertainty: Terminology

Accuracy, Precision and Error

- **Accuracy** describes how **correct** – how close to the *true answer* – the results are.
- **Precision** describes how **repeatable** they are.
- **Systematic errors** are **repeated in the same way** throughout an investigation, such as using a balance incorrectly in the same way for each measurement. This can be corrected. **Precision** describes how **repeatable** they are.
- **Random error** cannot easily be corrected as it affects measurements differently.

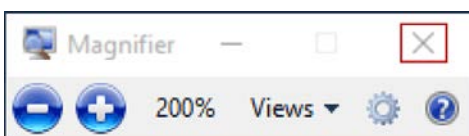


	Results A	Results B	Results C
Accuracy	Low	High	Low
Precision	High	High	Low
Systematic error	High	None	No
Random Error	No	None	High

Image source: Bishop, M. *Precision vs Accuracy* (Fig 1.12). From *Preparatory Chemistry* (ebook) via http://preparatorychemistry.com/Bishop_Book_1_eBook.pdf

Accuracy, Precision and Error

- **Accuracy** describes how **correct** – how close to the *true answer* – the results are.
- **Precision** describes how **repeatable** they are.
- **Systematic errors** are **repeated in the same way** throughout an investigation, such as using a balance incorrectly in the same way for each measurement. This can be corrected. **Precision** describes how **repeatable** they are.
- **Random error** cannot easily be corrected as it affects measurements differently.



	Results A	Results B	Results C
Accuracy	Low	High	Low
Precision	High	High	Low
Systematic error	High	None	No
Random Error	No	None	High

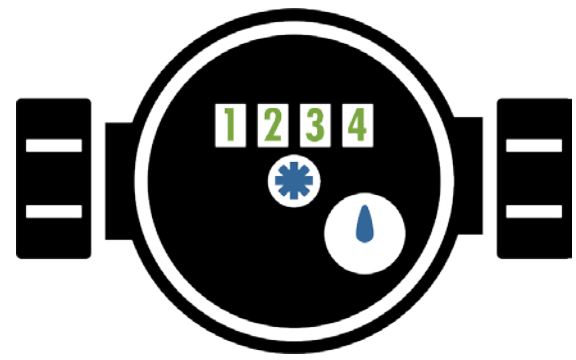
THE EFFECT OF ERRORS

الرعاية الرسمي
OFFICIAL SPONSOR



مؤسسة الكويت للتقنية والقياس
Kuwait Foundation for Technology and Metrology

Example:



+1%

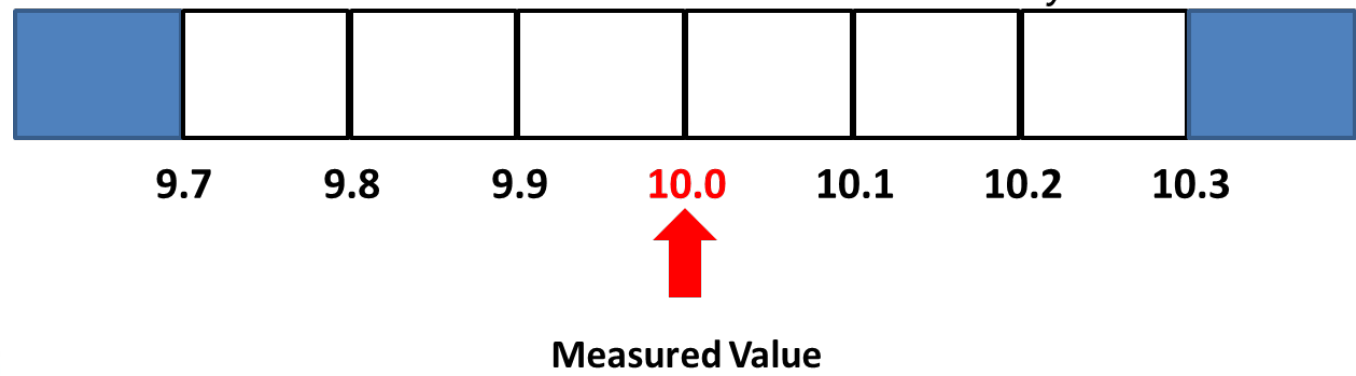
Over-reads by 1% you will lose \$10,000 every day



EXPRESSING UNCERTAINTY!

This is a measure of the likelihood that the **True Value** of a measurement lies in the defined **Uncertainty Interval**. In industry, the confidence level is usually set at **95%**.

An illustration of measurement uncertainty

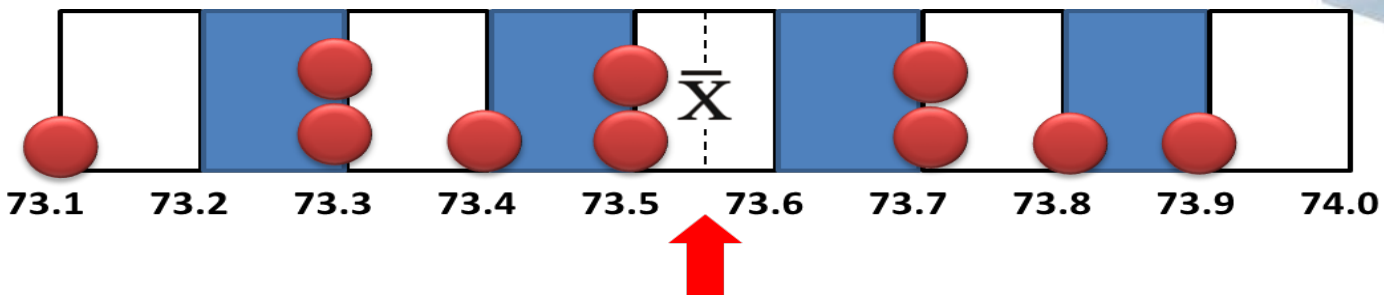


Uncertainty at
95%
Confidence is
3%.

95% confident: true value of this measurement lies between **9.7** and **10.3** m³/hr.

10.0 ± 0.3 @ 95% confidence

Type A analysis



1. Arithmetic mean

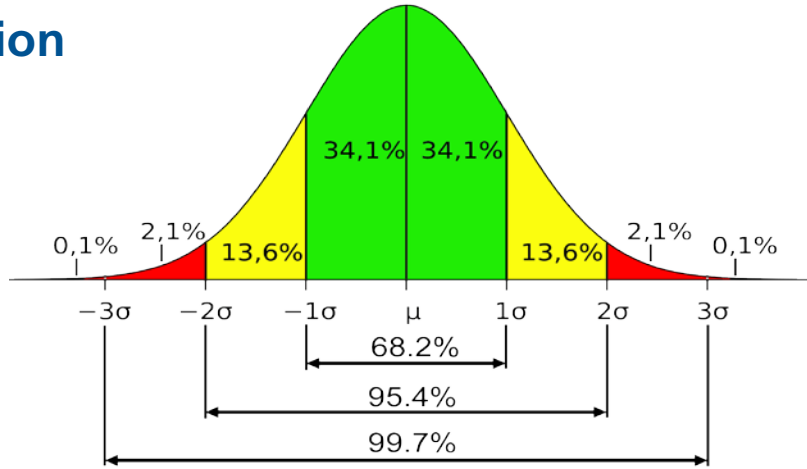
$$\bar{X} = \frac{\sum X}{N}$$

$$S = \sqrt{\frac{\sum (X - \bar{X})^2}{N}}$$

2. Spread or standard deviation

where S = the standard deviation of a sample,
 Σ means "sum of,"
 X = each value in the data set,
 \bar{X} = mean of all values in the data set,
 N = number of values in the data set.

3. Normal or Gaussian Distribution



CALCULATION METHOD

Arithmetic mean

Suppose that a turbine meter is used to measure the flow of water from a borehole. Readings are taken every two hours in the course of a single day and are (in m³/hr)

X ₁	X ₂	X ₃	X ₄	X ₅	X ₆	X ₇	X ₈	X ₉	X ₁₀	X ₁₁	X ₁₂
126.4	133.5	129.5	137.8	123.2	128.6	130.7	131.2	135.6	126.9	127.4	133.9

$$\text{Mean: } \bar{X} = \frac{\sum X}{N} = 130.4 \text{ m}^3/\text{hr}$$

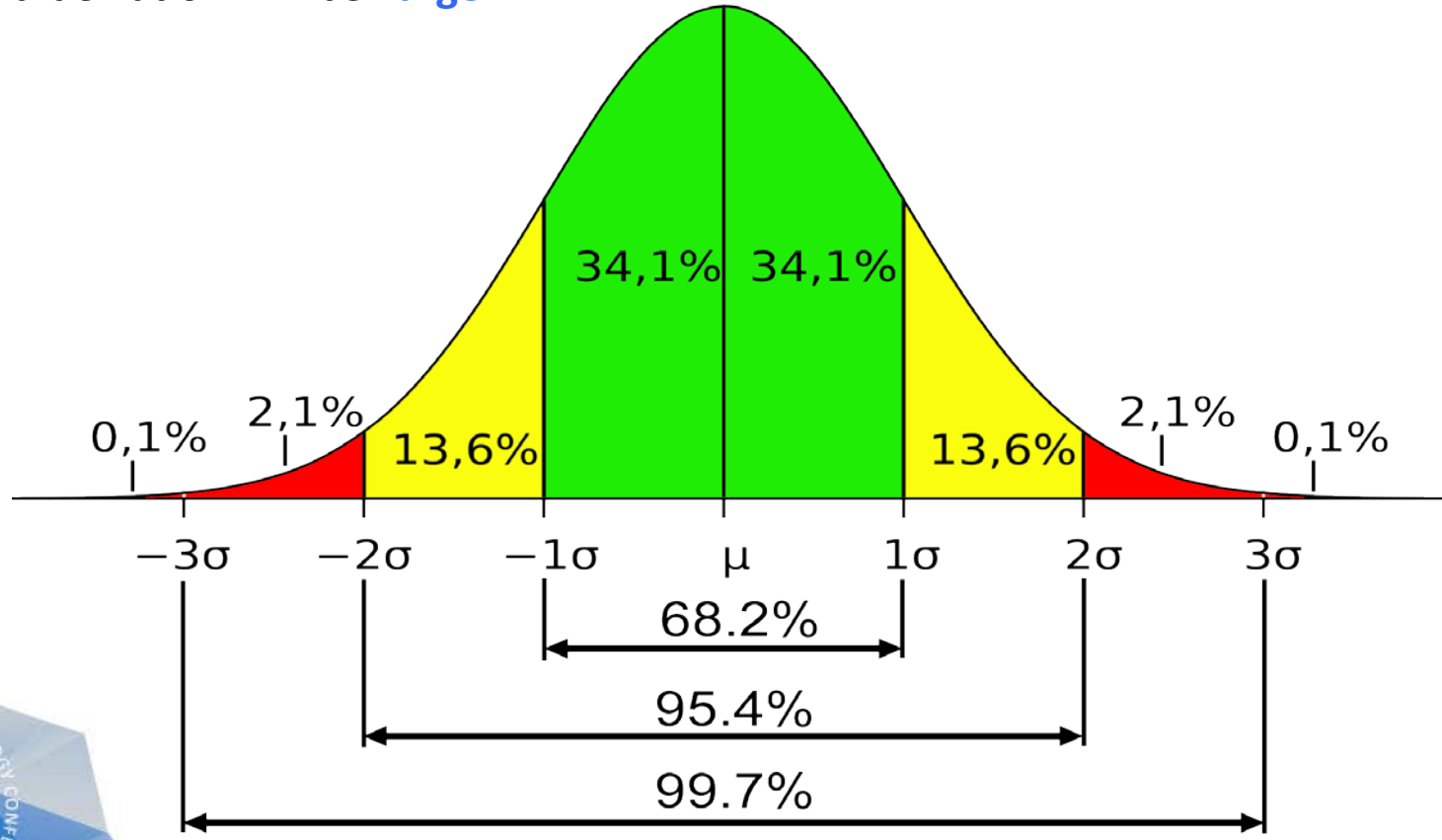
useful to know what the spread of the measurements is.

CALCULATION METHOD

2. Standard Deviation (σ)

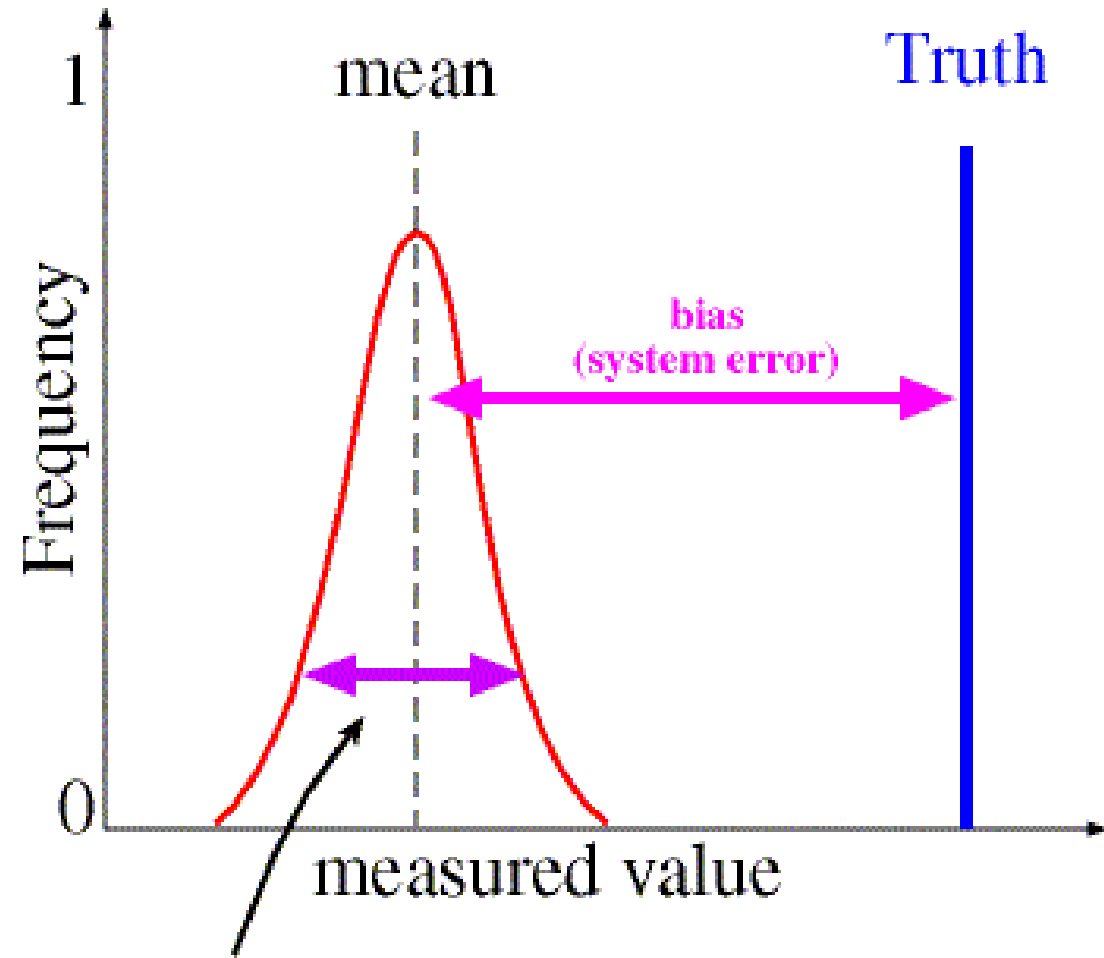
It's a unit of measure & shows the **Variation** in **Data**.

If the data is **Close** together, the standard deviation will be **Small**. If the data is spread out, the standard deviation will be **Large**.



CALCULATION METHOD

Standard Deviation



Precision (uncertainty)
also referred to as random error



CALCULATION METHOD

2. Standard Deviation σ

Suppose that a turbine meter is used to measure the flow of water from a borehole. Readings are taken every two hours in the course of a single day and are (in m³/hr)

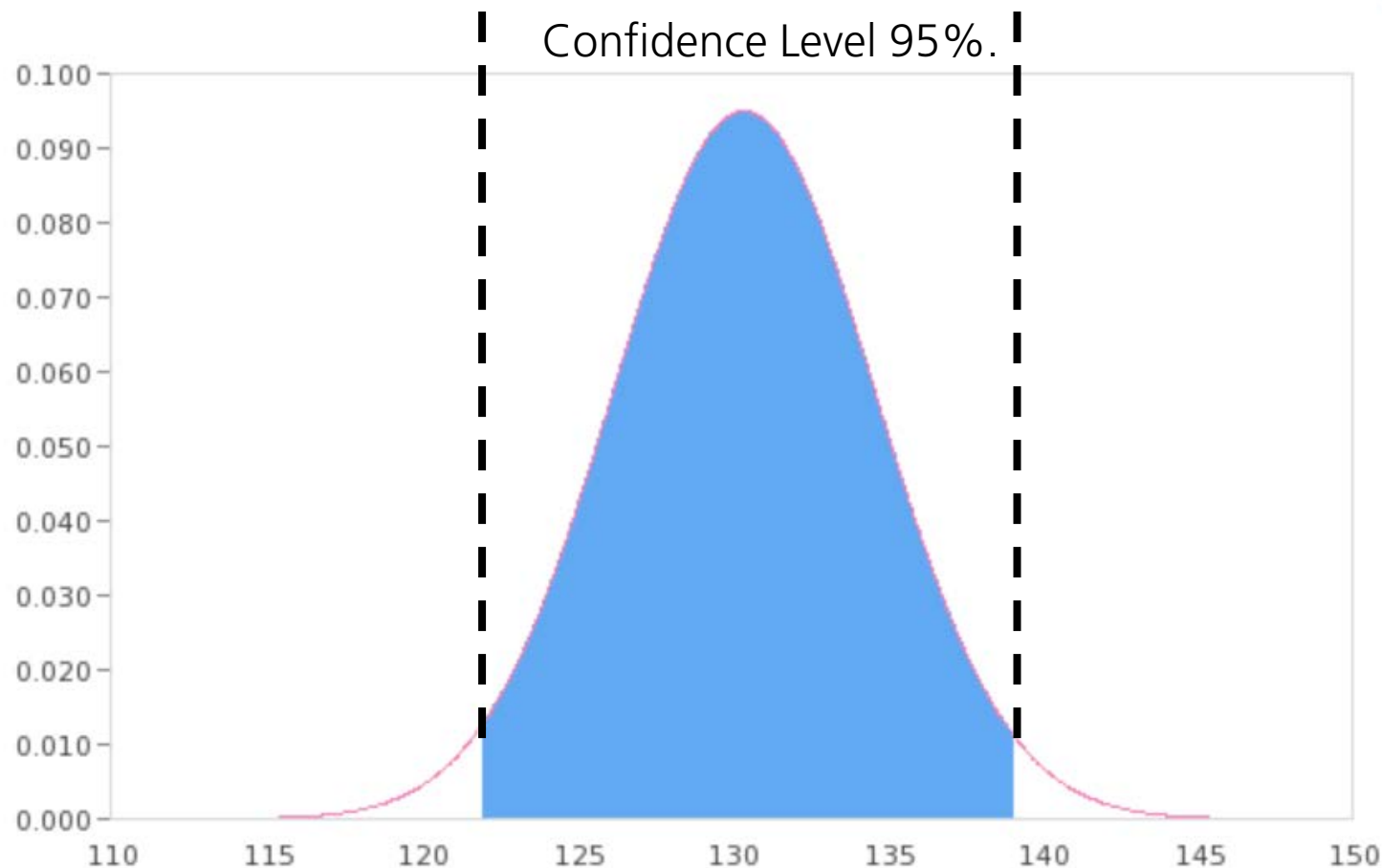
X ₁	X ₂	X ₃	X ₄	X ₅	X ₆	X ₇	X ₈	X ₉	X ₁₀	X ₁₁	X ₁₂
126.4	133.5	129.5	137.8	123.2	128.6	130.7	131.2	135.6	126.9	127.4	133.9

$$\text{STDEV: } \sigma = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}} = 4.2 \text{ m}^3/\text{hr}$$

Mean: **130.4 ± 4.2** m³/hr

CALCULATION METHOD

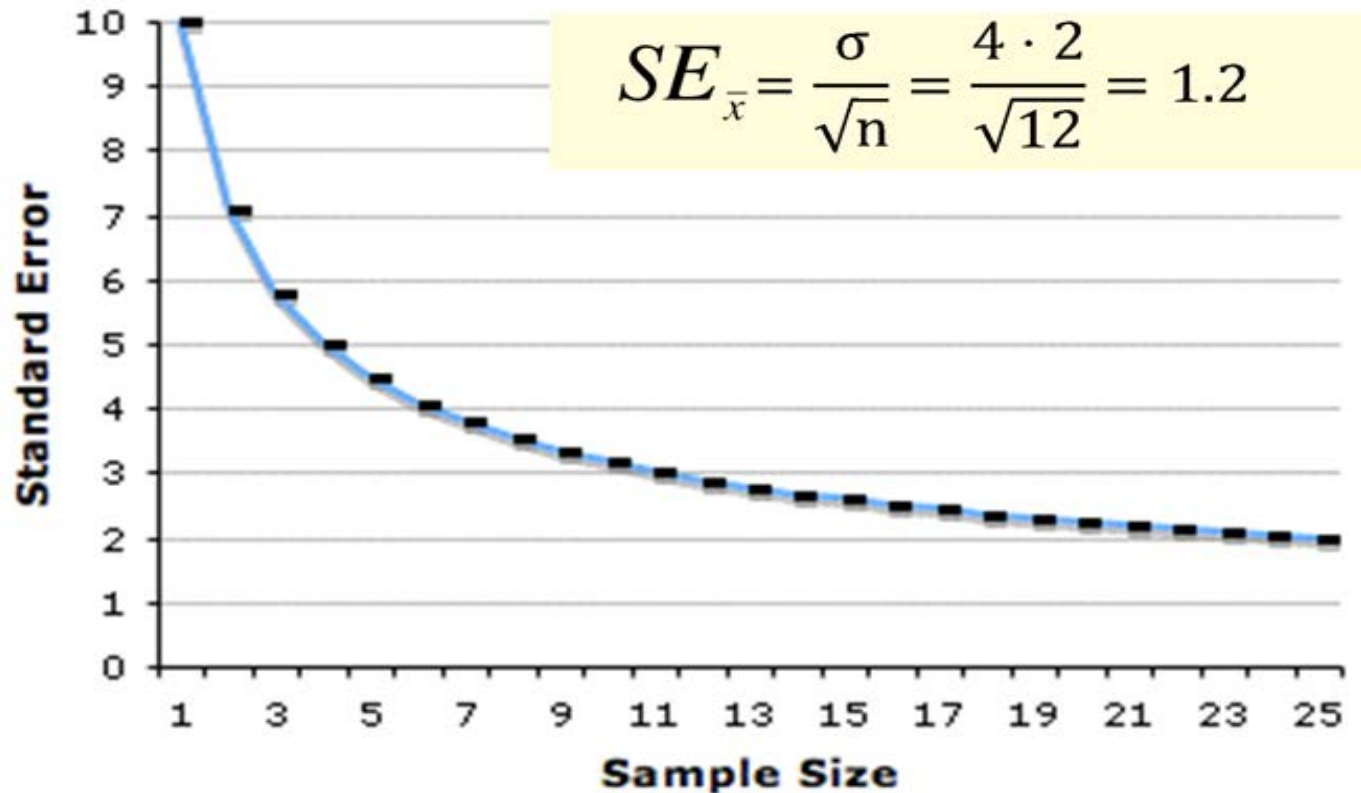
3. Normal Distribution



Standard Error of the Mean

Difference between **SEM** & **SD**:

- Standard deviation - it is a measure of data dispersion.
- Standard Error of the mean - refers to the probability that sample means, not individual data points, differ from the true population mean



Conclusion

الراعي الرسمي
OFFICIAL SPONSOR



مؤسسة الكويت للتقنية والقياس
Kuwait Foundation for Technology and Metrology

Standard Deviation and Standard Error of the Mean

However, Often it is **impossible** to assess the **magnitude** of the **uncertainty** from **repeated** measurements and have to be **quantified** using other **means**.

For example, these could be:

- The uncertainty quoted on a calibration certificate
- Engineering judgement based on experience of a measurement system
- Manufacturer's specifications



Flow Measurement Uncertainty: Standard Deviation and Standard Error of the Mean

Questions & Discussions

Flow Measurement Uncertainty: Standard Deviation and Standard Error of the Mean



*Thank you all
for your
time & attention
Bassam Al-Otaibi*